



## Spread Sheets for Laterals Spacing Design Application on Mit Kenana Area in Egypt

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### *Author's contribution*

*The sole author designed, analyzed and interpreted and prepared the manuscript.*

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### **ABSTRACT**

Mit Kenana area, 40 km North of Cairo, represents the eastern fringes of the Nile Delta in Egypt. Existing laterals spacing design of Mit Kenana area is reviewed. Then spread sheets are employed to obtain laterals spacing, which is referred to as spread sheet design. Microsoft Excel software, as instance for spread sheets, is employed to get the laterals spacing design of steady state subsurface drainage systems. The most suitable and popular Hooghoudt equation is used to get the spacing L, including the equivalent depth. Given data are depth to the impermeable layer, radius of the pipe lateral, hydraulic conductivities of the soil above and below drain level, elevation of the water table midway between the drains, and drainage rate. The lateral spacing L is assumed. Calculations are done through the spread sheet and the final result of L is obtained. Check for the obtained L is established with respect to the assumed value. Also, another check is employed for the equivalent depth  $d_e$ .

Almost identical results are accomplished by spread sheet design compared with the existing design. Laterals spacing design for steady state subsurface drainage systems employing spread sheets is efficient, accurate, quick, easy and simple.

*Keywords: Spread sheets; subsurface drainage; steady state; laterals; equivalent depth.*

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The lateral spacing design is established and the subsurface drainage system is accomplished for Mit Kenana area [5]. This design is referred to as existing design in this paper. Fig. 2 shows the principle of the subsurface drainage infrastructure of the area.

For the Nile Delta in Egypt, including Mit Kenana area, the water table depth of 0.8 m achieves good conditions for the cultivated crops [6]. Also, the drainage rate of 0.0012 m/day is acceptable.

### 2.2 Equations Employed in the Study

The movement of water into the drains is mainly affected by the hydraulic conductivity of the soil and drain spacing, depth, and size. The study employed the most suitable and popular Hooghoudt equation [7] for drainage design (Eqn. 1)

$$Q L^2 = 8 K_b (D_i - D_d) (D_d - D_w) + 4 K_a (D_d - D_w)^2 \quad (1)$$

Where

- Q = steady state drainage discharge rate (m/day)
- L = spacing between the drains (m)
- $K_b$  = hydraulic conductivity of the soil below drain level (m/day)
- $d_e$  = equivalent depth, a function of L,  $(D_i - D_d)$ , and r
- $D_i$  = depth of the impermeable layer (m)
- $D_d$  = depth of the drains (m)
- $D_w$  = steady state depth of the water table midway between the drains (m)
- $K_a$  = hydraulic conductivity of the soil above drain level (m/day)
- $r_0$  = drain radius (m)

To account for the extra head loss due to radial flow to the drains, two simplifications were followed in Hooghoudt theory. The first was assuming an imaginary impervious layer above the real one, which decreases the thickness of the layer through which the water flows towards the drains. The second was treating horizontal and radial flow to drains as an equivalent flow to imaginary ditches with their bottoms on an imaginary impervious layer at a reduced depth. In other words, the equivalent depth ( $d_e$ ) represents an imaginary thinner soil layer through which the same amount of water will flow horizontally per unit time as in the actual situation. In equation 1, replacing the term  $(D_i - D_d)$  by  $(d_e)$ ,

$$Q L^2 = 8 K_b d_e (D_d - D_w) + 4 K_a (D_d - D_w)^2 \quad (2)$$

To determine the equivalent depth, a relationship was derived by Hooghoudt between the equivalent depth ( $d_e$ ), the spacing (L), the depth to the impervious layer ( $D_i - D_d$ ), and the radius of the drain ( $r_0$ ). To simplify this relationship, tables were established for the most common sizes of drain pipes, from which the equivalent depth ( $d_e$ ) can be attained.

Exact solutions for the equivalent depth required for Hooghoudt equation can be calculated from the following two equations, where  $D = (D_i - D_d)$  [8].

$$\text{For } D < L/4, \quad d_e = \frac{D}{\frac{8D}{\pi L} \ln \frac{D}{\pi r_0} + 1} \quad (3)$$

$$\text{For } D > L/4, \quad d_e = \frac{\pi L}{8 \ln \frac{L}{\pi r_0}} \quad (4)$$

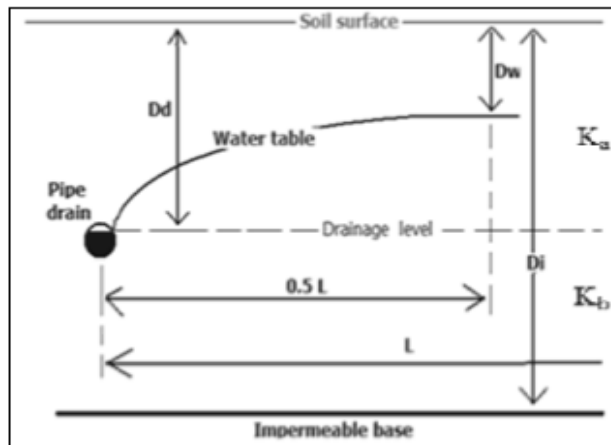


Fig. 2. Principle of subsurface drainage infrastructure at Mit Kenana area

### 2.3 Spread Sheets for Laterals Spacing Design of Steady State Subsurface Drainage Systems

Microsoft Excel software, as instance for spread sheets, is employed to get the laterals spacing design of steady state subsurface drainage systems. Equation 2 is used to get the spacing L, substituting by equation 3 to obtain the equivalent depth.

For the hypothetical case shown in Table 1, given data are D, r<sub>0</sub>, K<sub>a</sub>, K<sub>b</sub>, h and Q, where:

- D : Depth to the impermeable layer, (D<sub>i</sub> - D<sub>d</sub>), m
- r<sub>0</sub> : Radius of the pipe lateral, m
- K<sub>a</sub> : Hydraulic conductivity of the soil above drain level, m/day
- K<sub>b</sub> : Hydraulic conductivity of the soil below drain level, m/day
- h : Elevation of the water table midway between the drains, (D<sub>d</sub> - D<sub>w</sub>), m
- Q : Drainage rate, m/day

Then, the lateral spacing L is assumed. Calculations are done through the spread sheet

and the final result of L is obtained. Check for the obtained L is established with respect to the assumed value. Also, another check is employed for the equivalent depth d<sub>e</sub>, where D/L < 0.25 as stated in equation 3.

As shown in Table 1, the depth to impermeable layer (D) is 2.5 m, the lateral pipe radius (r<sub>0</sub>) is 0.1 m, hydraulic conductivities of the soil above and below drain level (K<sub>a</sub> and K<sub>b</sub>) are the same with the value of 1 m/day, elevation of the water table midway between the drains (h) is 0.2 m, and drainage rate (Q) is 0.001 m/day.

It is assumed first that the lateral spacing (L<sub>assumed</sub>) is 50 m. Then calculations through the spread sheet obtain a value of 58.29 m for the spacing (L) with 16.5% difference with respect to the assumed value. Other values are assumed for L till difference with respect to the assumed value becomes close to zero. Thus the spread sheets design for lateral spacing is 59 m, with only 0.19% difference with respect to the assumed value. Also the check for the equivalent depth (d<sub>e</sub>) is satisfied, where the value of D/L is less than 0.25.

**Table 1. Spread sheet for laterals spacing design of steady state subsurface drainage systems**

<b>Given</b>	D, m	2.5	2.5	2.5	2.5	2.5
	r <sub>0</sub> , m	0.1	0.1	0.1	0.1	0.1
	K <sub>a</sub> , m/day	1	1	1	1	1
	K <sub>b</sub> , m/day	1	1	1	1	1
	h, m	0.2	0.2	0.2	0.2	0.2
	Q, m/day	0.001	0.001	0.001	0.001	0.001
	<b>Assumed</b>	L <sub>assumed</sub> , m	50	55	58	<b>59</b>
<b>Calculated</b>		25	25	25	25	25
		3.218875	3.218875	3.218875	3.218875	3.218875
		8.208133	8.208133	8.208133	8.208133	8.208133
		4.708133	4.708133	4.708133	4.708133	4.708133
		0.235406	0.214006	0.202936	0.199497	0.196172
		1.235406	1.214006	1.202936	1.199497	1.196172
	d <sub>e</sub> , m	2.023625	2.059297	2.078247	2.084206	2.09
		0.16	0.16	0.16	0.16	0.16
		3.237800	3.294876	3.325195	3.334730	3.344000
		3.397800	3.454876	3.485195	3.494730	3.504000
	3397.800	3454.876	3485.195	3494.730	3504.000	
<b>Results</b>	L, m	58.2906	58.77819	59.03554	59.11624	59.19459
	Check L	16.5813	6.869449	1.785421	0.197028	-1.34234
	Check de	0.05	0.045454	0.043103	0.042372	0.041666
Check L = ((L-L <sub>assumed</sub> )/L <sub>assumed</sub> )*100					Check de:	D/L < 0.25

**2.4 Spread Sheets for Laterals Spacing Design for the Mit Kenana Area**

Spread sheets are employed to obtain laterals spacing for the Mit Kenana area, which is referred to as spread sheets design. Twenty two different laterals spacing designs are calculated according to the data of Mit Kenana area. These designs are included in Table 2. Also, three spread sheets designs are shown in Tables 3, 4 and 5 as samples for this technique.

**3. RESULTS AND DISCUSSION**

Three samples for spread sheets design are illustrated in Tables 3, 4 and 5. For each table, given data are the depth to impermeable layer ( $D = D_i - D_d$ ), the lateral pipe radius ( $r_0 = 0.1$  m), hydraulic conductivities of the soil above and below drain level ( $K_a = K_b = 3$  m/day), elevation of the water table midway between the drains ( $h$ ), and drainage rate ( $Q = 0.0015$  m/day). The values of ( $D$ ) and ( $h$ ) are varying according to the location within the area.

**Table 2. Spread sheets design of laterals spacing for Mit Kenana area**

Depth of Impermeable layer ( $D_i$ ), m	Laterals spacing, m		
	$D_d=1.0$ m, $h=0.2$ m	$D_d=1.2$ m, $h=0.3$ m	$D_d=1.4$ m, $h=0.3$ m
1.20	31	34	---
1.35	37	38	---
1.70	50 *	55	46
1.80	52	59	51 *
2.00	58	66	59
3.00	77	93	88
4.50	97	119	116
10.00	137	174	172 *

\* Spread sheets that obtained these results are shown in Tables 3, 4 and 5

**Table 3. Spread sheets design, depth of impermeable layer is 1.7 m, drain depth is 1.0 m, and elevation of the water table midway between the drains is 0.2 m**

<b>Given</b>	D, m	0.7	0.7	0.7	0.7
	$r_0$ , m	0.1	0.1	0.1	0.1
	$K_a$ , m/day	3	3	3	3
	$K_b$ , m/day	3	3	3	3
	h, m	0.2	0.2	0.2	0.2
	Q, m/day	0.0015	0.0015	0.0015	0.0015
	<b>Assumed</b>	Lassumed, m	30	49	<b>50</b>
<b>Calculated</b>		7	7	7	7
		1.9459101	1.9459101	1.9459101	1.9459101
		4.9620709	4.9620709	4.9620709	4.9620709
		1.4620709	1.4620709	1.4620709	1.4620709
		0.034115	0.0208867	0.020469	0.0200676
		1.034115	1.0208867	1.020469	1.0200676
	$d_e$ , m	0.6769073	0.6856784	0.6859591	0.686229
		0.48	0.48	0.48	0.48
		3.2491551	3.2912564	3.2926037	3.2938992
		3.7291551	3.7712564	3.7726037	3.7738992
	2486.1034	2514.171	2515.0691	2515.9328	
<b>Results</b>	L, m	49.86084	50.141509	50.150465	50.159075
	Check L	66.202801	2.3296107	0.3009301	-1.6488724
	Check $d_e$	0.0233333	0.0142857	0.014	0.0137255
Check L = $((L-L_{assumed})/L_{assumed}) * 100$					Check $d_e$ : $D/L < 0.25$

**Table 4. Spread sheets design, depth of impermeable layer is 1.8 m, drain depth is 1.4 m, and elevation of the water table midway between the drains is 0.3 m**

<b>Given</b>	D, m	0.4	0.4	0.4
	r <sub>0</sub> , m	0.1	0.1	0.1
	K <sub>a</sub> , m/day	3	3	3
	K <sub>b</sub> , m/day	3	3	3
	h, m	0.3	0.3	0.3
	Q, m/day	0.0015	0.0015	0.0015
<b>Assumed</b>	Lassumed, m	50	<b>51</b>	52
<b>Calculated</b>		4	4	4
		1.3862944	1.3862944	1.3862944
		3.5350506	3.5350506	3.5350506
		0.0350506	0.0350506	0.0350506
		0.0002804	0.0002749	0.0002696
		1.0002804	1.0002749	1.0002696
	d <sub>e</sub> , m	0.3998879	0.3998901	0.3998922
		1.08	1.08	1.08
		2.8791927	2.8792085	2.8792237
		3.9591927	3.9592085	3.9592237
	2639.4618	2639.4723	2639.4825	
<b>Results</b>	L, m	51.375692	51.375795	51.375894
	Check L	2.7513849	0.7368532	-1.2002041
	Check de	0.008	0.0078431	0.0076923
Check L = ((L-Lassumed)/Lassumed)*100		Check de: D/L < 0.25		

**Table 5. Spread sheets design, depth of impermeable layer is 10.0 m, drain depth is 1.4 m, and elevation of the water table midway between the drains is 0.3 m**

<b>Given</b>	D, m	8.6	8.6	8.6	8.6
	r <sub>0</sub> , m	0.1	0.1	0.1	0.1
	K <sub>a</sub> , m/day	3	3	3	3
	K <sub>b</sub> , m/day	3	3	3	3
	h, m	0.3	0.3	0.3	0.3
	Q, m/day	0.0015	0.0015	0.0015	0.0015
<b>Assumed</b>	Lassumed, m	90	155	<b>172</b>	173
<b>Calculated</b>		0.3142857	0.3142857	0.3142857	0.3142857
		27.363636	27.363636	27.363636	27.363636
		3.309215	3.309215	3.309215	3.309215
		0.2432323	0.1412317	0.1272727	0.126537
		0.8049081	0.467366	0.4211728	0.4187383
		1.8049081	1.467366	1.4211728	1.4187383
	d <sub>e</sub> , m	4.7647857	5.8608419	6.0513401	6.061724
		1.08	1.08	1.08	1.08
		34.306457	42.198062	43.569648	43.644413
		35.386457	43.278062	44.649648	44.724413
	23590.971	28852.041	29766.432	29816.275	
<b>Results</b>	L, m	153.59353	169.85889	172.52951	172.6739
	Check L	70.659473	9.5863784	0.3078554	-0.1884978
	Check de	0.095556	0.055484	0.05	0.049711
Check L = ((L-Lassumed)/Lassumed)*100		Check de: D/L < 0.25			

The lateral spacing is assumed first ( $L_{assumed}$ ), then calculations through the spread sheet obtain another value for the spacing (L). The percentage difference between (L) and ( $L_{assumed}$ ) with respect to ( $L_{assumed}$ ) is done to check (L). Other values are assumed for (L) till the difference becomes close to zero.

Also the check for the equivalent depth ( $d_e$ ) is satisfied, where the value of (D/L) has to be less than 0.25.

As shown in Tables 3 and 2, depth to impermeable layer (D) is 0.7 m ( $D = D_1 - D_d = 1.7 - 1.0$ ). It is assumed first that the lateral spacing ( $L_{assumed}$ ) is 30 m. After calculations through the spread sheet, the required spacing is 50 m with only 0.3% difference with respect to the assumed value. The check for the equivalent depth ( $d_e$ ) is satisfied, where the value of (D/L) is 0.014 (less than 0.25).

**Table 6. Existing and spread sheets design for laterals spacing [Drain Depth ( $D_d$ ) = 1.0 m & Elevation of water table midway between drains (h) = 0.2 m]**

Depth of impermeable layer ( $D_1$ ), m	Laterals spacing, m	
	Existing design	Spread sheet design
1.20	30	31
1.35	37	37
1.70	50	50
1.80	52	52
2.00	58	58
3.00	77	77
4.50	97	97
10.00	137	137

Similarly, as shown in Tables 4 and 2, depth to impermeable layer (D) is 0.4 m ( $D = D_1 - D_d = 1.8 - 1.4$ ). It is assumed first that the lateral spacing ( $L_{assumed}$ ) is 50 m. After calculations through the spread sheet, the required spacing is 51 m with only 0.7% difference with respect to the assumed value. The check for the equivalent depth ( $d_e$ ) is satisfied, where the value of (D/L) is 0.0078 (less than 0.25).

Finally, as shown in Tables 5 and 2, depth to impermeable layer (D) is 8.6 m ( $D = D_1 - D_d = 10.0 - 1.4$ ). It is assumed first that the lateral spacing ( $L_{assumed}$ ) is 90 m. After calculations through the spread sheet, the required spacing is 172 m with only 0.3% difference with respect to

the assumed value. The check for the equivalent depth ( $d_e$ ) is satisfied, where the value of (D/L) is 0.05 (less than 0.25).

Existing design of Mit Kenana area is reviewed according to the design data. Both existing design and spread sheets design are tabulated in Tables 6, 7 and 8.

**Table 7. Existing and spread sheets design for laterals spacing [Drain Depth ( $D_d$ ) = 1.2 m & Elevation of water table midway between drains (h) = 0.3 m]**

Depth of impermeable layer ( $D_1$ ), m	Laterals spacing, m	
	Existing design	Spread sheet design
1.20	34	34
1.35	37	38
1.70	55	55
1.80	59	59
2.00	66	66
3.00	93	93
4.50	120	119
10.00	174	174

**Table 8. Existing and spread sheets design for laterals spacing [Drain Depth ( $D_d$ ) = 1.4 m & Elevation of water table midway between drains (h) = 0.3 m]**

Depth of impermeable layer ( $D_1$ ), m	Laterals spacing, m	
	Existing design	Spread sheet design
1.70	46	46
1.80	50	51 *
2.00	59	59
3.00	88	88
4.50	116	116
10.00	172	172 *

As shown in Table 6, eight different laterals spacing designs are calculated according to the data of Mit Kenana area. Similarly, Table 7 includes eight different laterals spacing designs. Finally, Table 8 contains six different laterals spacing designs.

From these obtained results, it can be seen that both existing design and spread sheets design are almost identical with negligible differences in limited designs.

The steady state condition is followed in Egypt, where the rate of recharge to the aquifer is

assumed to be steady and equals the discharge of the drain. So, the water table position does not change as long as the recharge continues [9].

Spread sheets are efficient, accurate, and simple way that can be applied to solve many issues in hydraulics and water resources. For instance, Microsoft Excel software, as a common popular spread sheet, was employed to get the best hydraulic trapezoidal sections for open channels with different side slopes [10]. Also, an additional solution was obtained concerning the velocity of water through the trapezoidal best hydraulic sections.

Many attempts were done to calculate the equivalent depth in order to get the laterals spacing for the subsurface drainage systems. Chieng et al. [11] introduced some graphs for the equivalent depth versus the depth to impermeable layer for a range of pipe sizes and spacing between laterals. Efficient values for the equivalent depth are obtained by the technique employed in this paper.

Also, a drain spacing formula has been derived considering the variation in flow and the area above the drain level in the radial flow zone [12]. The extent of radial flow zone is found to be  $2/\pi$  times the thickness of soil layer below the drains. Hooghoudt equation based on equivalent depth is accurate enough to be used for drain spacing, but the computed water surface profile in the radial flow zone differs considerably from that computed by the new method.

#### 4. CONCLUSIONS

Laterals spacing design for steady state subsurface drainage systems employing spread sheets is efficient, accurate, quick, easy and simple. It can be widely used to get the required spacing between the laterals (field drains). Applying this technique on Mit Kenana area in Egypt obtained almost identical results compared with the existing design. This technique can be applied to get the laterals spacing design quickly and accurately. It can be also used to obtain efficiently the equivalent depth for steady state subsurface drainage systems.

#### COMPETING INTERESTS

Author has declared that no competing interests exist.

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